

# Homework 13

Due Tuesday, November 24, 11:59 PM

## Definitions

(a) State:

- (i) The definition of one-point compactification of a space  $X$ .
- (ii) The definition of closure of a subset of a topological space  $X$ .
- (iii) The definition of interior of a subset of a topological space  $X$ .
- (iv) The definition of what it means for a subset of a topological space  $X$  to be dense.
- (v) The definition of a base (or basis) of a topology.

## Proof(s)

Prove that  $S^n$  is homeomorphic to the one-point compactification of  $\mathbb{R}^n$ .

## Canvas True/False Questions:

Indicate whether each of the following statements is true or false:

1. If  $X$  is compact and Hausdorff and connected, then  $X^+$  is connected.
2. If  $X$  is not Hausdorff, then  $X^+$  is Hausdorff.
3.  $\mathbb{Q}$  is a dense subset of  $\mathbb{R}$  when  $\mathbb{R}$  is given the standard topology.
4.  $\mathbb{Q}$  is a dense subset of  $\mathbb{R}$  when  $\mathbb{R}$  is given the discrete topology.
5.  $\mathbb{Q}$ , given the subspace topology inherited from  $\mathbb{R}$  with the standard topology, is connected.
6.  $\mathbb{Q}$ , given the subspace topology inherited from  $\mathbb{R}$  with the standard topology, is path-connected.