

## Writing Assignment 10

Due Friday, October 30, 11:59 PM

This is secretly asking you for a proof, but you may treat it as a writing assignment if that helps you think through the problem better.

Let  $A \subset X$  and  $B \subset Y$ . If  $X$  and  $Y$  are topological spaces, then  $A$  and  $B$  can be given the subspace topology. Accordingly, the set  $A \times B$  can be given the product topology. Call this topology  $\mathcal{T}$ .

On the other hand, consider the subset  $A \times B \subset X \times Y$  and give  $A \times B$  the subspace topology. Call it  $\mathcal{T}'$ .

Are  $\mathcal{T}$  and  $\mathcal{T}'$  the same topology?

Explore, write; explain your thoughts.