

**Extra Credit 3.**

Let  $X, Y$ , and  $Z$  be sets.

**Notation 2.1.** Let  $f$  be a function from  $X$  to  $Y$ . Then, if  $x$  is an element of  $X$ , we will as usual write  $f(x)$  for the element of  $Y$  that  $f$  assigns to  $x$ .

Now let  $g$  be a function from  $Y$  to  $Z$ .

**Remark 2.2.** Based on the notation above, you know what  $g(y)$  means when  $y$  is an element of  $Y$ . Thus, you know what  $g(f(x))$  means when  $x$  is an element of  $X$ .

**Definition 2.3.** We will define the *composition* of  $g$  and  $f$  to be the assignment from  $X$  to  $Z$  which takes any  $x \in X$  and assigns to it  $g(f(x))$ .

We will write  $gf$ , or  $g \circ f$ , for the composition of  $g$  and  $f$ .

True or false: If  $f$  and  $g$  are bijections, then the composition  $gf$  is also a bijection.

If this is true, tell me why, giving a full but concise explanation.

If it is false, please explain why; for instance, by providing a counter-example.